

# Magnetoacoustic waves propagating along a dense slab and Harris current sheet in the solar atmosphere

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# OUTLINE

- **Introduction:**

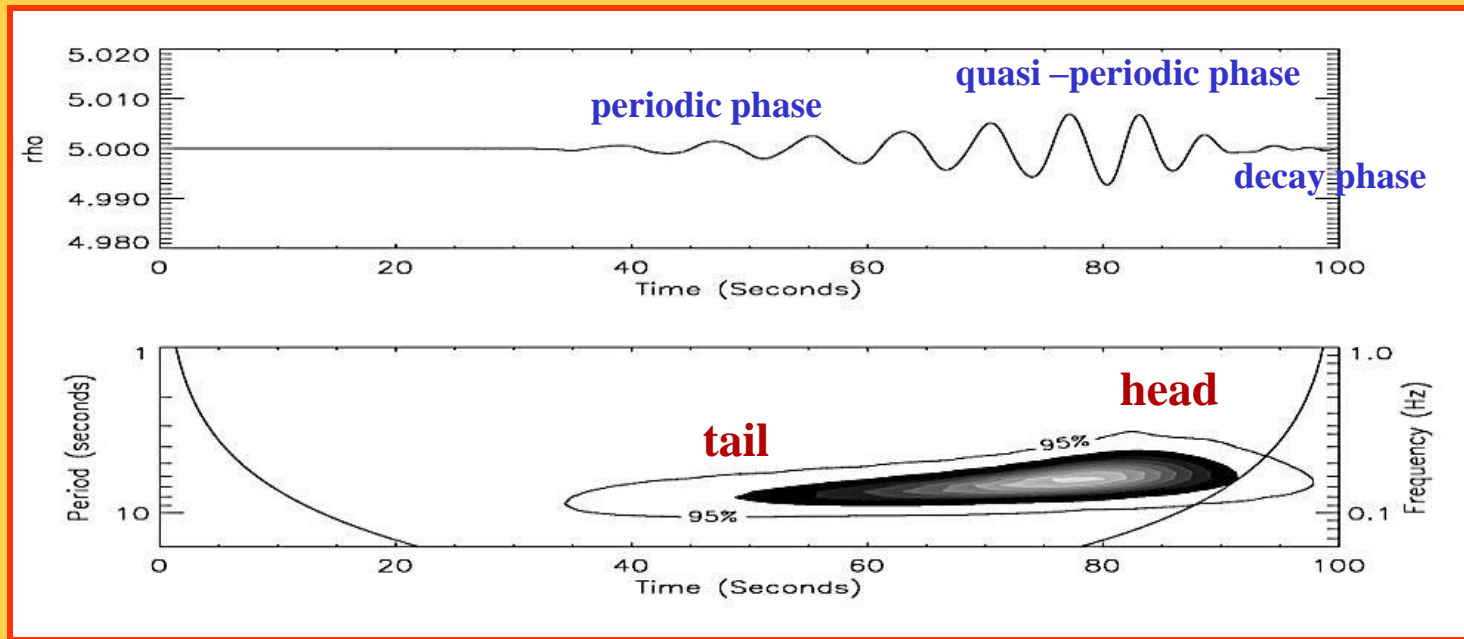
- \* basic magnetoacoustic waves features
- \* basic features of the dense slab & Harris current sheet

- **2D MHD numerical simulations:**

- \* parameters of the simulations
- \* spatial and temporal analysis of waves
- \* example of observed magnetoacoustic waves
- \* mutual interactions between two waves

- **Results and Conclusions**

# Impulsively Generated Propagating Magnetoacoustic Waves



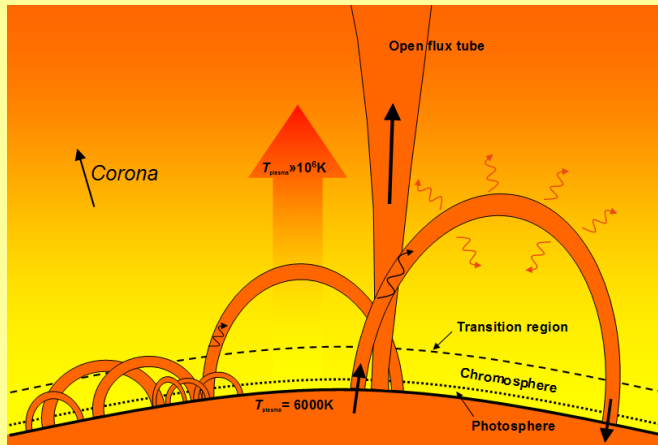
characteristic **WAVELET TADPOLE**  
signature where narrow spectrum **tail**  
precedes the broadband **head**

from Nakariakov et al., 2004, MNRAS

# Impulsively Generated Magnetoacoustic Waves

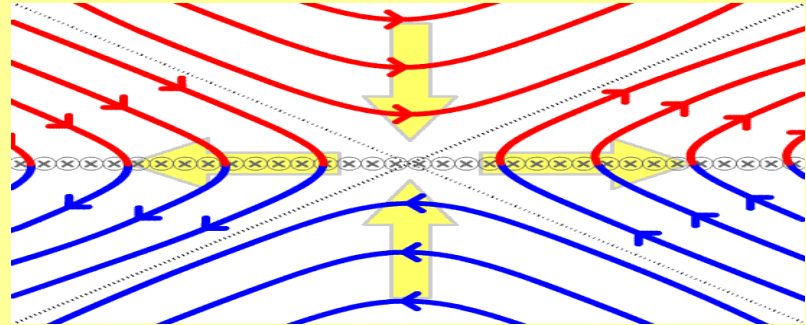
## DENSE SLAB

≈ simulation of a coronal loop



waves propagate along a loop

## HARRIS CURRENT SHEET

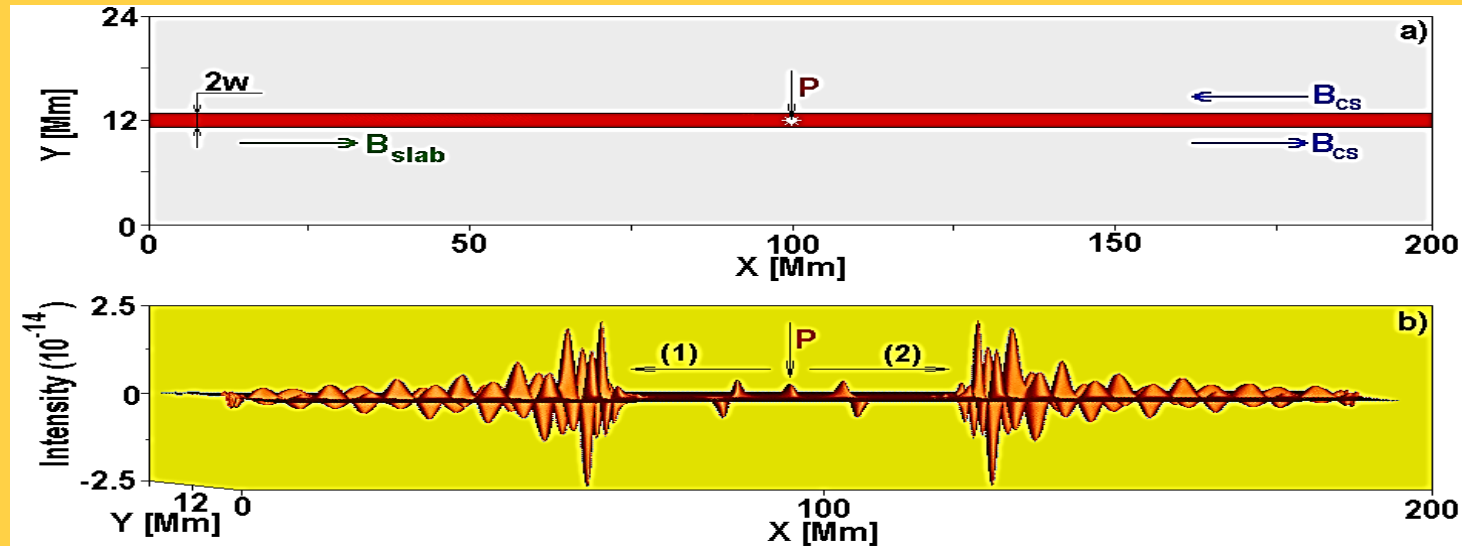


magnetic reconnection:

- 4 magnetic domains at the figure center,
- field lines with plasma flow inward from above and below the separator, reconnect, and spring outward horizontally,
- CS perpendicular to the field lines at the figure center,
- Harris: magnetic field profile is given by

$$\mathbf{B} = B_0 \tanh(x/L) \mathbf{e}_z$$

waves propagate along the CS



numerical box: **length = 200 Mm,** **width = 24 Mm**

uniform **cell size:  $dx = dy = 80$  km**

red strip = waveguide (slab/current sheet),  $w$  = half-width of waveguide,

**P = perturbation point,**

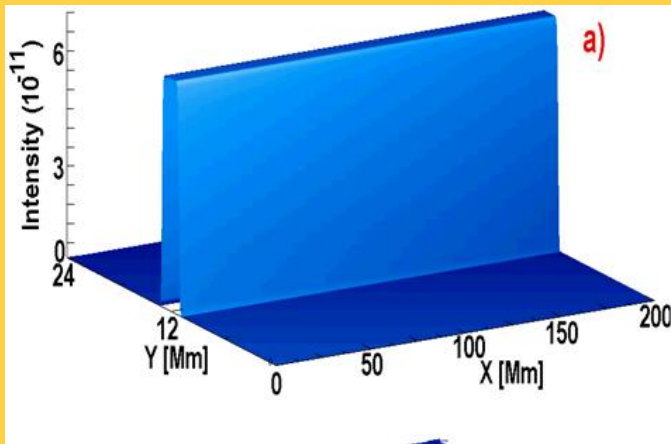
magnetic field configuration: **green arrow =  $B_{slab}$**

**blue arrows =  $B_{CS}$  (current sheet)**

plasma dynamics described by full set of ideal time-dependent MHD equations

time step  $\Delta t = 0.044$  s

**example of waveguide: DENSITY SLAB (e.g. coronal loops)**



**mass density  $\rho$  profile**

$$\rho(X, Y) = \rho_0 + (\rho_{\text{slab}} - \rho_0) \cdot \text{sech}^2 \left\{ \left[ \frac{(Y - Y_P)}{w} \right]^\alpha \right\}$$

**power index  $\alpha = 8$  determines  
the steepness of the profile**

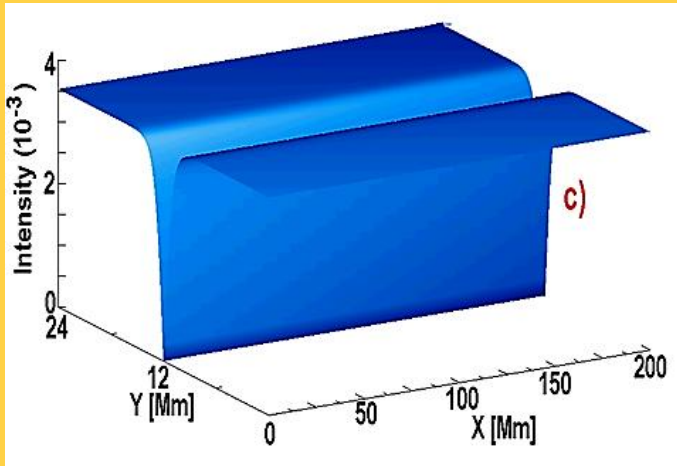
(Nakariakov & Roberts, SolPhys. 1995)

**magnetic field  $B_{\text{slab}}$  is parallel to the X-axis and constant in the whole simulation region ( $B_{\text{slab}} = 3.5 \times 10^{-3}$  T)  
electron density  $n_e = 10^{16} \text{ m}^{-3}$**

**selected the parameters in/out of slab:  
mass density  $\rho_{\text{in}} = 6.69 \times 10^{-11} \text{ kg m}^{-3}$   
mass density  $\rho_{\text{out}} = 6.08 \times 10^{-12} \text{ kg m}^{-3}$   
temperature  $T_{\text{in}} = 0.45 \text{ MK}$ ,  
 $T_{\text{out}} = 5 \text{ MK}$**

**Alfvén velocity  $v_{A-\text{in}} = 0.39 \text{ Mm s}^{-1}$   
 $v_{A-\text{out}} = 1.28 \text{ Mm s}^{-1}$   
sound velocity  $c_{s-\text{in}} = 0.11 \text{ Mm s}^{-1}$   
 $c_{s-\text{out}} = 0.37 \text{ Mm s}^{-1}$**

# example of waveguide: CURRENT SHEET



magnetic field  $B$  profile

$$\mathbf{B} = B_{\text{out}} \tanh \left[ \frac{(Y - Y_P)}{w} \right] \hat{e}_X$$

selected parameters in the center  $c$ ,  
at  $Y = w$  and in/out of the current sheet:

magnetic field  $B_{\text{out}} = 3.5 \times 10^{-3} \text{ T}$

mass density  $\rho_c = 6.69 \times 10^{-11} \text{ kg m}^{-3}$

$\rho_w = 3.32 \times 10^{-11} \text{ kg m}^{-3}$

$\rho_{\text{out}} = 6.08 \times 10^{-12} \text{ kg m}^{-3}$

temperature =  $T = 5 \text{ MK}$

sound speed  $c_s = 0.37 \text{ Mm s}^{-1}$

Alfven velocity  $v_{A-c} = 0$

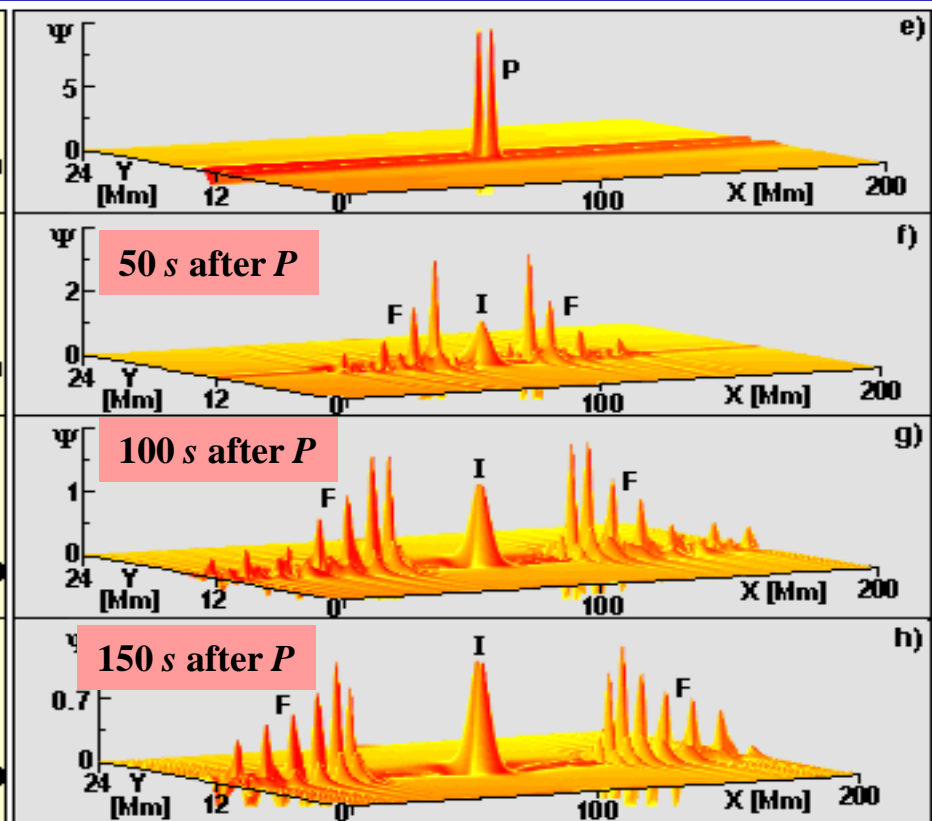
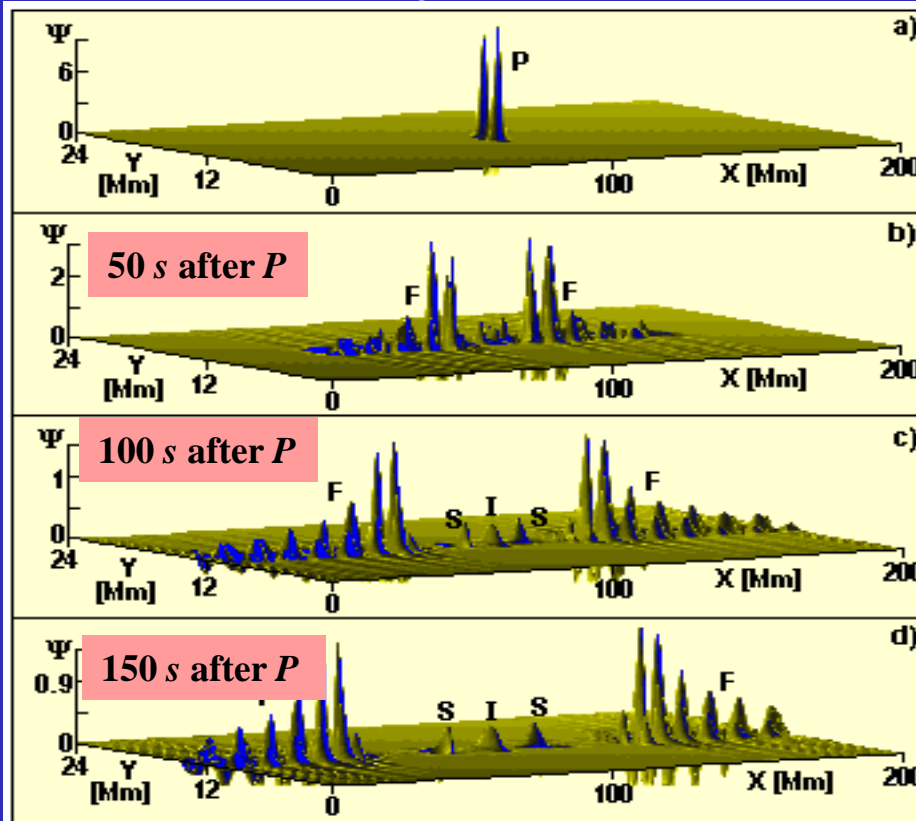
$v_{A-w} = 0.40 \text{ Mm s}^{-1}$

$v_{A-\text{out}} = 1.28 \text{ Mm s}^{-1}$

# Time evolution of the magnetoacoustic waves (mass density):

## density slab

## Harris current sheet



**P** = initial perturbation

**F** = fast wave train

**S** = slow wave

**I** = nonpropagating peak of entropy mode in situ of perturbation

Mészárosová et al., 2014, ApJ



# Role of the waveguide half-width $w$ [Mm] & distance from perturbation $P$ [Mm]

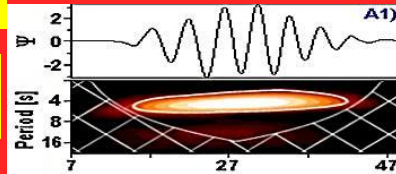
density  
slab

distance

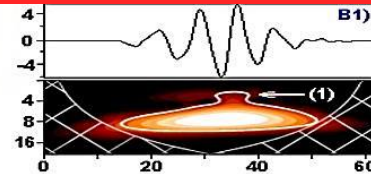
10 Mm

50 Mm

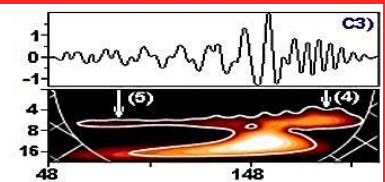
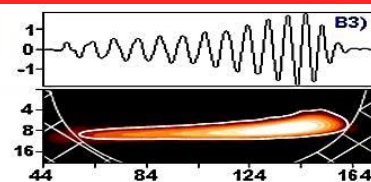
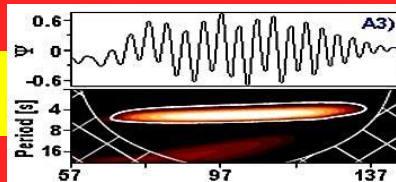
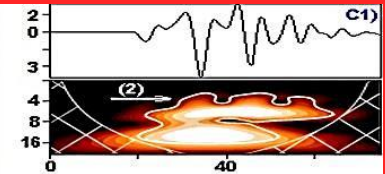
$w = 0.5$  Mm



$w = 1.0$  Mm



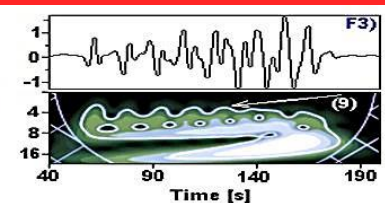
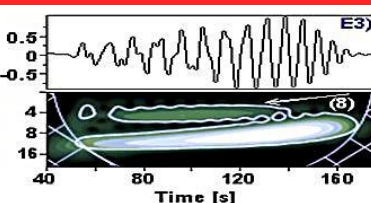
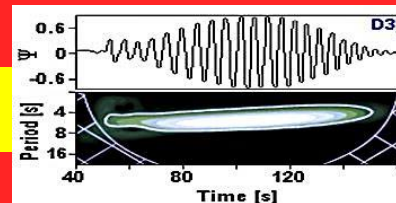
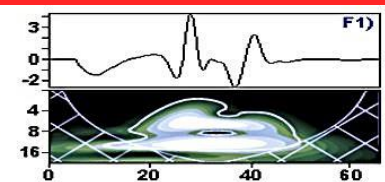
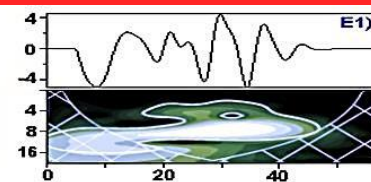
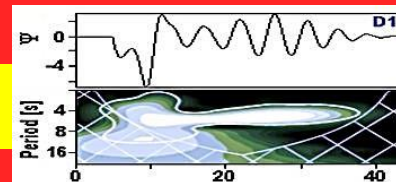
$w = 2.0$  Mm



current  
sheet

10 Mm

50 Mm

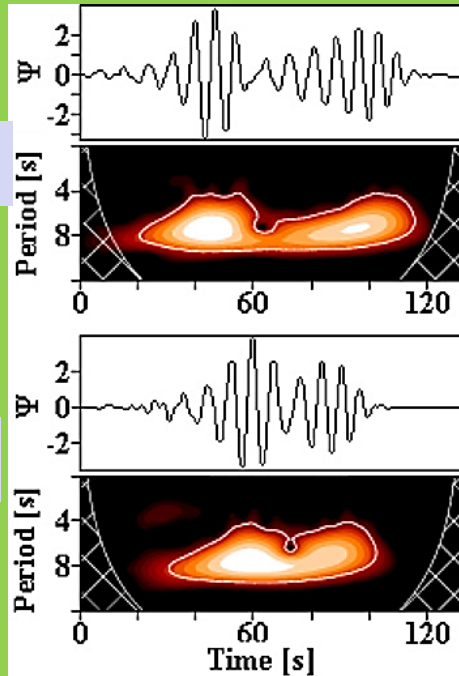


Mészárosóvá et al., 2014, ApJ

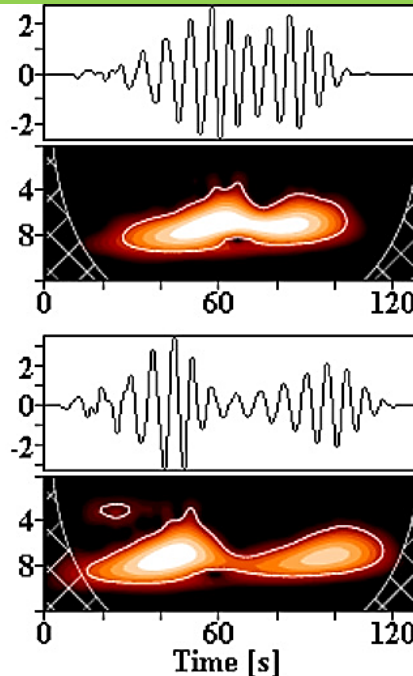
**Time series and their wavelet spectra corresponding to a mutual interaction between two fast waves in the dense slab**

**→ superposition (temporary merger) of both waves**

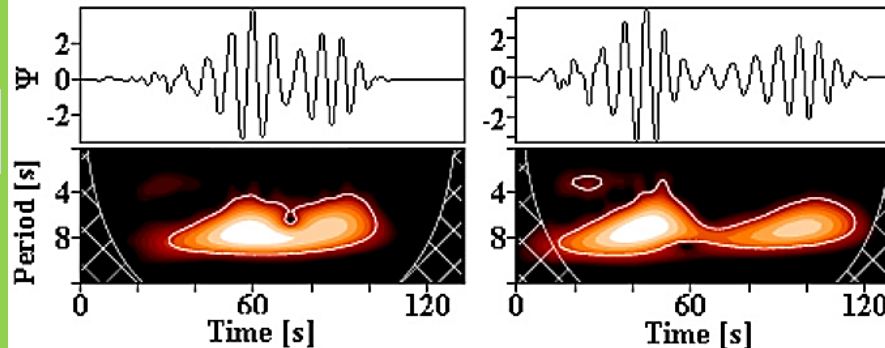
**d = 90 Mm**



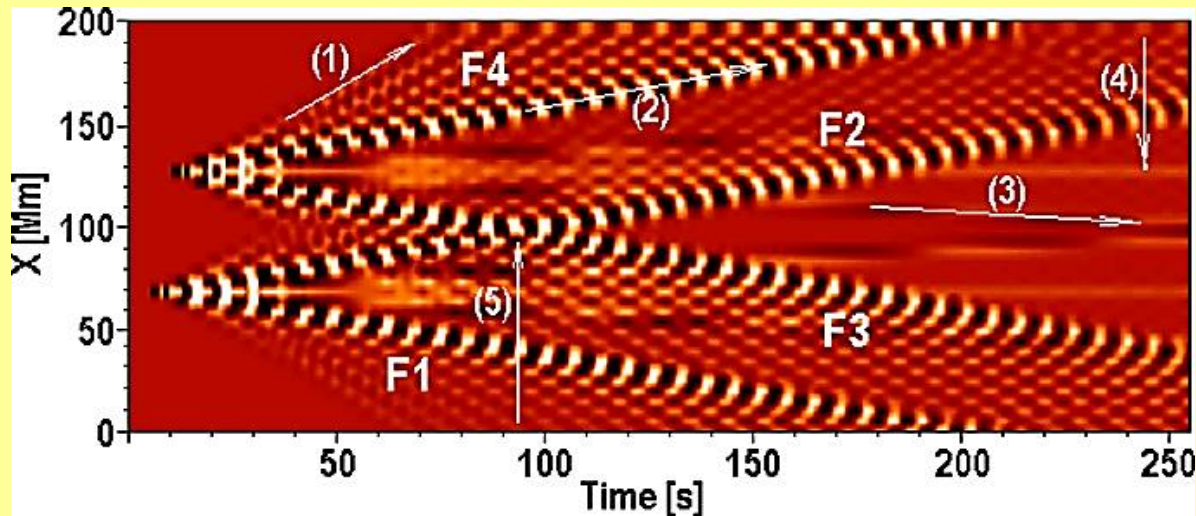
**d = 105 Mm**



**d = 110 Mm**



**d = distance from a perturbation place**



**Dynamic spectrum**  
of time series  
collected at selected  
points  $X = 0 - 200$  Mm  
along the density slab  
(spatial step = 5 Mm)

**1<sup>st</sup> perturbation** generated 5 s after starting time at point  $X = 70$  Mm

→ **fast waves F1 and F2**

**2<sup>nd</sup> perturbation** generated 10 s after starting time at point  $X = 130$  Mm

→ **fast waves F3 and F4**

**Arrow 1:** fastest spectral components of the **fast wave F4** (velocity = 1.0 Mm/s)

**Arrow 2:** slowest spectral components of the **fast wave F4** (velocity = 0.35 Mm/s)

**Arrow 3:** one of **slow waves** (velocity = 0.1 Mm/s)

**Arrow 4:** nonpropagating peak of the **entropy mode**

**Arrow 5:** waves F2 and F3 propagate toward the waveguide center ( $X = 100$  Mm) and they interact at a time of 93 s

Mészárosóvá et al., 2014, ApJ

Our computed velocities agree with those theoretically predicted by Roberts et al. (1984) – for the initial values of the MHD simulation:

**Alfvén velocity out of the dense slab**  $v_{A-out} = 1.28$  Mm/s should correspond to the fastest components of the fast wave train

**Alfvén velocity in the dense slab**  $v_{A-in} = 0.39$  Mm/s should correspond to the slowest components of the fast wave train

**sound velocity in the dense slab**  $c_{s-in} = 0.11$  Mm/s should correspond to the slow magnetoacoustic wave

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results of the MHD simulations for a dense slab:

fastest spectral components of the **fast wave F4** (velocity = 1.0 Mm/s)

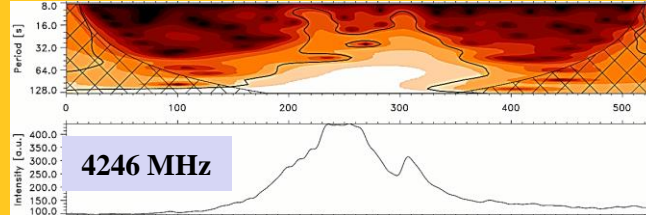
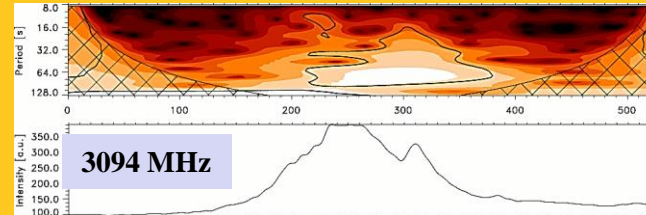
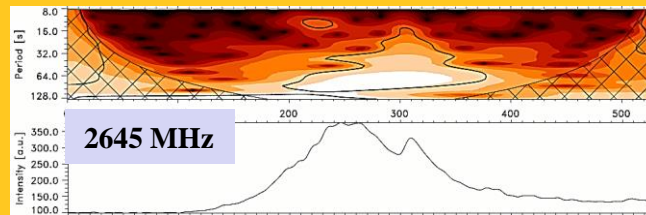
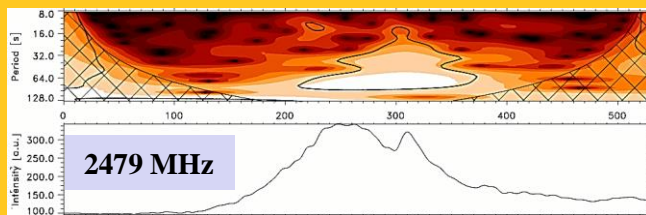
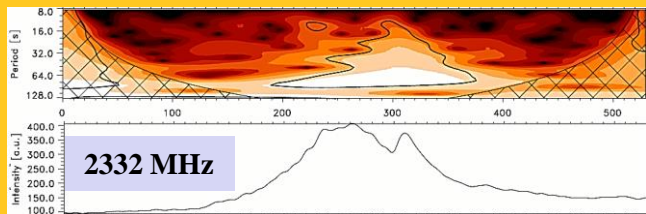
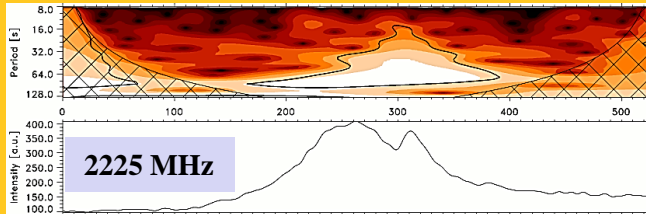
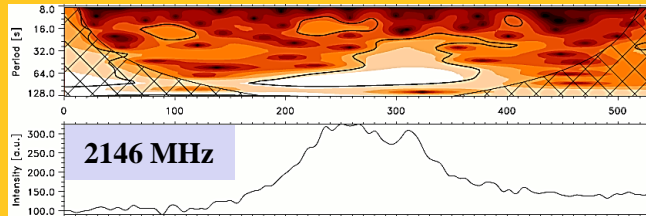
slowest spectral components of the **fast wave F4** (velocity = 0.35 Mm/s)

**slow waves** (velocity = 0.1 Mm/s)

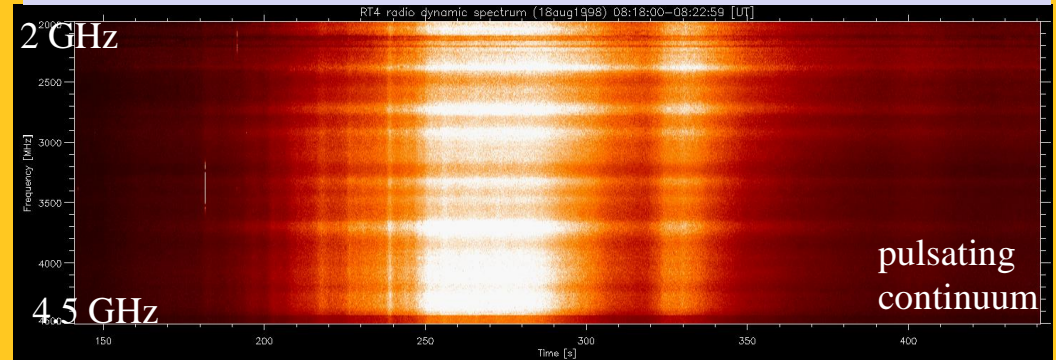
Mészárosová et al., 2014, ApJ

# Magnetoacoustic Waves:

# Observations



radio dynamic spectrum, Ondřejov observatory  
18 Aug 1998, 2.0 – 4.5 GHz, 8:18 – 8:23 UT



at all frequencies: wave period  $P = 94$  s  
additional head structures  $\rightarrow$  waveguide  $\approx$  loop

about 4 GHz:  
shorter tadpole tail  
closer to perturbation

## Conclusions:

- **The dense slab and current sheet guide the fast waves in a similar way. They differ in guiding of the slow waves. The difference comes from the different magnetic fields and temperature structures of these waveguides.**
- **Each fast wave forms a wave train. The slow wave propagates as a single peak. We found a nonpropagating wave at the site of the initial perturbation in both types of the waveguide.**
- **For cases with the narrow waveguide ( $w = 0.5 \text{ Mm}$ ) the tadpole heads were suppressed. For waveguide half-width  $> 1 \text{ Mm}$  there are additional structures of tadpole heads. In the dense slab case these additional structures were always delayed after the tadpole head maximum. The current sheet case is the opposite.**
- **mutual interactions of waves generated by two perturbations:**  
**Wavelet spectra of the fast waves depends on the evolution states of the wave trains of both waves at the time of their interaction.**



**Thank you  
for your attention!**